

## HIGH SPEED ADDER

### BACKGROUND OF THE INVENTION

#### 1. Field of the Invention

5           The present invention relates to an adder, and more particularly to an adder that operates at a high speed.

#### 2. Description of the Related Art

          In recent years, computers are becoming faster and faster. Therefore, a higher speed arithmetic circuit is required and  
10   a technique for increasing an operating speed of an adder serving as an important part thereof becomes important. A large number of techniques for realizing a high speed adder have been known. Of those, a conditional sum adder has been widely known as one of the highest-speed adders.

15           Fig. 1 is a circuit diagram showing a 4-bit conditional sum adder of a first conventional example described in, particularly, Fig. 6 in Kuo-Hsing Cheng et al., "The improvement of conditional sum adder for low power applications", 1998. IEEE ASIC Conference Proceedings, pp. 131-134. As shown in Fig. 1,  
20   in the first conventional example, when a binary number (A<sub>3</sub>, A<sub>2</sub>, A<sub>1</sub>, A<sub>0</sub>) is added to a binary number (B<sub>3</sub>, B<sub>2</sub>, B<sub>1</sub>, B<sub>0</sub>), each of conditional cells 111 in a first circuit stage 21 generates both provisional bit sum signals and provisional carry signals and outputs them. Here, the provisional sums include a bit sum  
25   signal (for example, S0<sub>1</sub>) with respect to the case where carry is produced from a low order bit and a bit sum signal (for example, S1<sub>1</sub>) with respect to the case where no carry is produced. In addition, the provisional carriers include a carry signal (for example, C0<sub>1</sub>) with respect to the case where carry is produced  
30   from a low order bit and a carry signal (for example, C1<sub>1</sub>) with

respect to the case where no carry is produced. In a second circuit stage 22, one of the two provisional sums and one of the two provisional carriers are selected by multiplexers (MUXs) 120 in accordance with a carry signal from a low order bit and transferred to a next stage. In a third circuit stage 23, actual bit sums  $S_0$  to  $S_3$  and an output carry signal  $C_{out}$  are generated by actual carry signals and outputted to the outside of the adder. According to the first conventional example, because the  $2^N$ -bit adder can be realized by  $(N+1)$  circuit stages, the high speed operation is possible. However, in the first conventional example, because the adder includes a large number of multiplexers and the number of wirings is large, power dissipation is large.

As an adder improved to reduce power dissipation, there is a conditional carry adder of a second conventional example described in, particularly, Fig. 7 in Kuo-Hsing Cheng et al., "The improvement of conditional sum adder for low power applications", 1998. IEEE ASIC Conference Proceedings, pp. 131-134. Fig. 2 is a circuit diagram of a 16-bit conditional carry adder. As shown in Fig. 2, in the second conventional example, each of conditional cells 101 (Fig. 4B is a circuit diagram) is different from the conditional cell 111 in the first conventional example. That is, each of the conditional cells 101 in a first circuit stage 31 generates an exclusive OR signal of two input bits (for example,  $S0_1$ ) and provisional carriers and outputs them. Here, the provisional carriers are composed of a pair of signals which are a carry signal with respect to the case where carry is produced from a low order bit and a carry signal with respect to the case where no carry is produced. In a second circuit stage 32 to a fifth circuit stage 35, each carry

signal to be sent to a next circuit stage is selected by a multiplexer (MUX) 120 and a carry selector 110 in accordance with a carry signal from a low order bit and transferred in succession. In a sixth circuit stage 36 including exclusive  
5 OR circuits 130, actual bit sums S\_1 to S\_15 are generated and outputted to the outside of the adder. According to the second conventional example, because only the provisional carriers may be generated and outputted and no provisional sums are required, the number of multiplexers (one carry selector is counted as  
10 two multiplexers) can be reduced. Accordingly, power dissipation at the time of operation can be reduced.

However, when the  $2^N$ -bit adder is realized in the second conventional example, (N+2) circuit stages are required. In the case of comparison using a 16-bit adder, although the number  
15 of circuit stages is five in the first conventional example, the number of circuit stages is six in the second conventional example. Therefore, because the number of logic stages in a critical path is increased by one stage, it is disadvantageous to increase a circuit operation speed.

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#### SUMMARY OF THE INVENTION

The present invention has been made in view of the above-mentioned circumstances. Therefore, an object of the present invention is to provide an adder that can operate in  
25 low power by reducing the number of unit circuits such as multiplexers and the number of wirings as compared with the first conventional example while a high speed operation at the same speed as in the first conventional example (that is, at a higher speed than in the second conventional example) is maintained.

30 According to the present invention, there is provided a

high speed adder in which provisional carriers composed of a pair of signals that indicate a case where carry is produced from a low order bit and a case where no carry is produced therefrom are generated in advance and an actual carrier is selected from the provisional carriers in accordance with selection information from the low order bit to increase a carrier transfer speed, the adder including: a carrier transfer path; and a plurality of converters, each of which converts the provisional carriers into provisional sums composed of a pair of signals that indicate the case where the carry is produced from the low order bit and the case where no carry is produced therefrom, the converters being provided on a predetermined portion of the carrier transfer path.

According to the adder of the first conventional example, the provisional carriers and the provisional sums are generated and transferred in the first circuit stage. In addition, according to the adder of the second conventional example, the provisional carriers are transferred to generate actual carry signals and all actual bit sums are collectively generated in a final circuit stage. In contrast to these, according to the adder of the present invention, in a circuit stage on the way to the transfer of the carriers, the provisional carriers are converted into the provisional sums and transported. According to the structure of the adder of the present invention, the number of multiplexers and the number of input and output wirings for the multiplexers can be reduced as compared with the adder of the first conventional example. In addition, the adder can be realized by the number of circuit stages smaller than that in the second conventional example.

The above and other related objects and features of the

present invention will be apparent by reading the following description with the accompanying drawings and novelty pointed out in the appended claims.

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#### BRIEF DESCRIPTION OF THE DRAWINGS

In order to fully understand the drawings used in the detailed description of the present invention, the respective drawings will be briefly described, in which:

Fig. 1 is a circuit diagram in the case where a conditional  
10 sum adder of a first conventional example is applied to a 4-bit adder;

Fig. 2 is a circuit diagram in the case where a conditional carry adder of a second conventional example is applied to a 16-bit adder;

15 Fig. 3 is a circuit diagram showing a 16-bit adder according to an embodiment of an adder of the present invention;

Fig. 4A shows an internal structure of a first circuit stage in the 16-bit adder and Fig. 4B is a circuit diagram showing a gate level of a conditional cell;

20 Fig. 5 shows an internal structure of a second circuit stage in the 16-bit adder;

Fig. 6A shows a multiplexer and Fig. 6B shows a carry selector;

25 Fig. 7 shows an internal structure of a third circuit stage in the 16-bit adder;

Fig. 8 shows an internal structure of a fourth circuit stage in the 16-bit adder; and

Fig. 9 shows an internal structure of a fifth circuit stage in the 16-bit adder.

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# DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

Hereinafter, a preferred embodiment of the present invention will be described in detail with reference to the drawings. Note that the following description is of a  
 5 representative embodiment of the present invention and the present invention is not limited to the following description in the interpretation thereof.

Fig. 3 is a circuit diagram showing a 16-bit adder according to an embodiment of an adder of the present invention. In the  
 10 adder shown in Fig. 3, as in the case of the second conventional example shown in Fig. 2, 16-bit input data (A<sub>15</sub> to A<sub>0</sub>) and (B<sub>15</sub> to B<sub>0</sub>) and an input carry signal Cin are inputted thereto and 16-bit sum output signals (S<sub>15</sub> to S<sub>0</sub>) indicating the sums thereof and an output carry signal Cout are outputted therefrom.  
 15 However, the adder shown in Fig. 3 is distinguished from the second conventional example by the following points. That is, the exclusive OR circuits that output actual bit sums S<sub>1</sub> to S<sub>8</sub> in the circuit stage 36 shown in Fig. 2 is included in a final stage, and, the exclusive OR circuits that output the actual  
 20 bit sums S<sub>9</sub> to S<sub>15</sub> are replaced by each of converters 140 in which provisional carriers composed of a pair of carry signals are inputted and converted into provisional sums composed of a pair of bit sum signals and the provisional sums are outputted.

Next, structures of the respective circuit stages will  
 25 be described in detail.

In a 2<sup>N</sup>-bit adder to which the present invention is applied, a first circuit stage includes (2<sup>N</sup>-1) conditional cells 101 and a full adder 100. Each of the conditional cells 101 is provided corresponding to the most significant bit to a bit larger than  
 30 the least significant bit by one bit, performs exclusive OR

calculation on corresponding bits of two input data which are inputted thereto, generates provisional carriers composed of a pair of signals that indicate the case where carry is produced from a low order bit and the case where no carry is produced, and outputs the provisional carriers. The full adder 100 generates an exclusive OR signal and a carry signal in accordance with the least significant bits of the two input data and an input carry signal, which are inputted thereto. The function of each of the conditional cells 101 and the function of the full adder 100 are the same as in the second conventional example.

Fig. 4A shows an internal structure of a first circuit stage 11 in the 16-bit adder shown in Fig. 3. The two input data are inputted to 15 ( $= 2^4 - 1$ ) conditional cells 101 and the full adder. Each of the conditional cells 101 is provided for each bit of the same digit from the most significant bit in the low order direction. The full adder is provided corresponding to the least significant bit. Each of the conditional cells 101 generates an exclusive OR signal of inputted two bits (for example, S0\_1). In addition, each of the conditional cells 101 generates a carry signal (for example, C0\_1) in the case where it is assumed that an input carry signal from a low order bit is 0 (that is, no carry is produced) and a carry signal (for example, C1\_1) in the case where it is assumed that the input carry signal from the low order bit is 1 (that is, carry is produced) and outputs the carry signals as provisional carriers composed of a pair of signals. Accordingly, exclusive OR signals S0\_1 to S0\_15, carry signals (C0\_1 to C0\_15) in the case where it is assumed that no carry is produced from the low order bit, and carry signals (C1\_1 to C1\_15) in the case where it is assumed that carry is produced from the low order

bit are outputted from the first circuit stage. The full adder 100 is used for the least significant bits. Bits  $A_0$  and  $B_0$  and an input carry signal  $C_{in}$  are simultaneously inputted to the full adder 100 and an actual bit sum  $S_0$  and an actual carry signal  $C_{out\_0}$  are outputted therefrom.

Fig. 4B is a circuit diagram showing an example of an internal structure of the conditional cell 101. The conditional cell 101 includes a first gate 102 that performs AND operation on inputted two input bits ( $A_i$ ,  $B_i$ ), a second gate 103 that performs OR operation on the inputted two input bits, a third gate 104 that inverts the output of the first gate 102, and a fourth gate 105 that performs AND operation on the output of the second gate 103 and the output of the third gate 104. The output of the first gate 102 is given as a first carry signal ( $C0_i$ ) which is the carry signal in the case where it is assumed that no carry is produced from the low order bit. The output of the second gate is given as a second carry signal ( $C1_i$ ) which is the carry signal in the case where it is assumed that the carry is produced from the low order bit. The output of the fourth gate is outputted as an exclusive OR signal ( $S0_i$ ) corresponding to a bit sum of the two input bits in the case where it is assumed that no carry is produced from the low order bit.

Of the second to  $n$ th circuit stages of the  $2^N$ -bit adder of the present invention, a  $(N-M+1)$ -th circuit stage specified by an integer  $M$  that satisfies  $1 \leq M < N$  is constructed as follows.

Fig. 5 shows an internal structure of a second circuit stage 12 in the 16-bit adder of the embodiment shown in Fig. 3. The second circuit stage 12 is a circuit stage in which  $(N-M+1) = 2$ . Accordingly, because  $N = 4$  in the 16-bit adder,  $M = 3$  is

obtained. In the second circuit stage 12, because  $(N-M) = 1$ , the circuit is divided in a virtual form into  $2^M (= 8)$  sub-circuits  $P2_1$  to  $P2_8$  corresponding to every  $2^{(N-M)} = 2$  bits of the input data.

5 In the case of such division, one multiplexer (MUX) 120 is provided corresponding to higher  $2^{(N-M-1)} (= 1)$  bits in the sub-circuit  $P2_1$  which is a first sub-arithmetic circuit, including inputs from  $2^{(N-M)}$ -th ( $=$  second) bits from the least significant bits  $A_0$  and  $B_0$  in the high order direction. The  
10 pair of signals  $C0_1$  and  $C1_1$  which are the outputs of the conditional cells 101 provided for corresponding bits in the first circuit stage 11 which is the preceding circuit stage and indicate the provisional carriers are inputted to the multiplexer. With respect to the multiplexer, a carry signal  $Cout_0$  which  
15 is outputted from the full adder 100 provided for bits in the first circuit stage 11, which correspond to  $(2^{(N-M-1)}+1)$ -th ( $=$  second) bits from the high order in the sub-circuit  $P2_1$  is inputted thereto as a selection signal. The multiplexer outputs a signal 300, which is an actual carry signal in accordance with the carry  
20 signal  $Cout_0$ .

Also, the  $(2^{(N-1)} - 2^{(N-M-1)}) (= 7)$  carry selectors 110 are provided corresponding to higher  $2^{(N-M-1)} (= 1)$  bit in the sub-circuit  $P2_8$  corresponding to a second sub-arithmetic circuit to which the signals  $C0_{15}$  and  $C1_{15}$  as the carry signals  
25 corresponding to the most significant bits  $A_{15}$  and  $B_{15}$  are inputted and in the corresponding sub-circuits of a third sub-arithmetic circuit including sub-circuits corresponding to the second sub-circuit  $P2_7$  and the second  $((= 2^M - 1) - \text{th}) (= \text{seventh})$  sub-circuit  $P2_2$  counted down from the sub-circuit  $P2_8$ . The pair  
30 of signals which are outputs of the conditional cells which are

provided for the corresponding bits in the first circuit stage 11 that is the preceding circuit stage are inputted to each of the carry selectors. In addition, the pair of selection signals which are the outputs of the conditional cells 101 provided for the bits in the first circuit stage 11, which correspond to  $(2^{(N-M-1)}+1)$ -th (= second) bits from the higher bits in the sub-circuit are inputted to each of the carry selectors. Each of the carry selectors in the second sub-arithmetic circuit ( $P2_8$ ) and the third sub-arithmetic circuit ( $P2_2$  to  $P2_7$ ) selects a pair of signal indicating provisional carriers or the provisional sums in the following circuit stage in accordance with the selection signals and outputs the selected signals.

In other words, the pair of signals  $C0_{15}$  and  $C1_{15}$  corresponding to higher order bits are inputted to the carry selector 110 included in the sub-circuit  $P2_8$ . Then, the carry selector 110 outputs a pair of signals 315 and 316 selected in accordance with the pair of signals  $C0_{14}$  and  $C1_{14}$  corresponding to  $(2^{(N-M-1)}+1)$ -th (= second) bits from the higher bits in the sub-circuit  $P2_8$ . Similarly, the pair of signals  $C0_{13}$  and  $C1_{13}$  corresponding to the high order bits are inputted to the carry selector 110 included in the sub-circuit  $P2_7$ . Then, the carry selector 110 outputs a pair of signals 311 and 312 selected in accordance with the pair of signals  $C0_{12}$  and  $C1_{12}$  corresponding to second bits from the higher order in the sub-circuit  $P2_7$ . In addition, the pair of signals  $C0_{11}$  and  $C1_{11}$  corresponding to the higher order bits are inputted to the carry selector 110 included in the sub-circuit  $P2_6$ . Then, the carry selector 110 outputs a pair of signals 309 and 310 selected in accordance with the pair of signals  $C0_{10}$  and  $C1_{10}$  corresponding to the second bits from the high order in the sub-circuit  $P2_6$ . In

addition, the pair of signals C0\_9 and C1\_9 corresponding to  
 the higher order bits are inputted to the carry selector 110  
 included in the sub-circuit P2<sub>5</sub>. Then, the carry selector 110  
 outputs a pair of signals 307 and 308 selected in accordance  
 5 with the pair of signals C0\_8 and C1\_8 corresponding to the second  
 bits from the higher order in the sub-circuit P2<sub>5</sub>. In addition,  
 the pair of signals C0\_7 and C1\_7 corresponding to the higher  
 order bits are inputted to the carry selector 110 included in  
 the sub-circuit P2<sub>4</sub>. Then, the carry selector 110 outputs a  
 10 pair of signals 305 and 306 selected in accordance with the pair  
 of signals C0\_6 and C1\_6 corresponding to the second bits from  
 the higher order in the sub-circuit P2<sub>4</sub>. In addition, the pair  
 of signals C0\_5 and C1\_5 corresponding to the higher order bits  
 are inputted to the carry selector 110 included in the sub-circuit  
 15 P2<sub>3</sub>. Then, the carry selector 110 outputs a pair of signals  
 303 and 304 selected in accordance with the pair of signals C0\_4  
 and C1\_4 corresponding to the second bits from the high order  
 in the sub-circuit P2<sub>3</sub>. In addition, the pair of signals C0\_3  
 and C1\_3 corresponding to the high order bits are inputted to  
 20 the carry selector 110 included in the sub-circuit P2<sub>2</sub>. Then,  
 the carry selector 110 outputs a pair of signals 301 and 302  
 selected in accordance with the pair of signals C0\_2 and C1\_2  
 provided for bits corresponding to the second bits from the higher  
 order in the sub-circuit P2<sub>2</sub>.

25 Also, the converter 140 is provided corresponding to a  
 lower  $2^{(N-M-1)}$  (= 1) bit in the sub-circuit P2<sub>8</sub> which is the second  
 sub-arithmetic circuit. The pair of signals C0\_14 and C1\_14  
 and the exclusive OR signal S0\_15 are inputted to the converter.  
 The pair of signals C0\_14 and C1\_14 are the outputs of the  
 30 conditional cell 101 provided for corresponding bits in the first

circuit stage 11 which is the preceding circuit stage and indicate the provisional carriers. The exclusive OR signal S0\_15 is outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11. Then, the  
 5 converter converts the inputted signals into a pair of signals 313 and 314 indicating the provisional sums and outputs the converted signals.

As shown in Fig. 6A, with respect to a multiplexer 120, a pair of input signals Cin0 and Cin1 are inputted thereto. One  
 10 of the pair of input signals Cin0 and Cin1 is selected in accordance with a selection signal Cin1s and outputted as an output signal Cout1. When the selection signal Cin1s is 1, Cin1 is outputted as the output signal Cout1. On the other hand, when Cin1s is 0, Cin0 is outputted as Cout1.

15 The carry selector 110 has the same function as the carry selector in the second conventional example as shown in Fig. 2. As shown in Fig. 6B, the carry selector 110 includes two multiplexers 350 and 351. When the pair of input signals Cin0 and Cin1 are inputted, the first multiplexer 351 selects one  
 20 of the pair of input signals Cin0 and Cin1 in accordance with the selection signal Cin0s which is one of the pair of selection signals Cin0s and Cin1s and outputs the selected signal as an output signal Cout0 which is one of a pair of output signals of the carry selector 110. When the pair of input signals Cin0  
 25 and Cin1 are inputted, the second multiplexer 350 selects one of the input signals Cin0 and Cin1 in accordance with the selection signal Cin1s which is the other of the pair of selection signals and outputs the selected signal as an output signal Cout1 which is the other of the pair of output signals of the carry selector  
 30 110. In the multiplexer 350, when Cin1s is 1, Cin1 is selected.

When Cin1s is 0, Cin0 is selected. In the multiplexer 351, when Cin0s is 1, Cin1 is selected. When Cin0s is 0, Cin0 is selected. Taking the carry selector included in the sub-circuit P2<sub>8</sub> as shown in Fig. 5 as an example, C0\_15 is inputted as Cin0 in Fig. 6B, C1\_15 is inputted as Cin1, C0\_14 is inputted as Cin0s, C1\_14 is inputted as Cin1s, the signal 315 is outputted as Cout0, and the signal 316 is outputted as Cout1.

The converter 140 will be described by using a converter included in the sub-circuit P2<sub>8</sub> as shown in Fig. 5 as an example.

10 The converter 140 is composed of a first exclusive OR circuit and a second exclusive OR circuit. When the signal C0\_14 which is one of the pair of signals C0\_14 and C1\_14 indicating the provisional carriers and the exclusive OR signal S0\_15 outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11 are inputted, the first exclusive OR circuit outputs the signal 313 which is one of the pair of signals 313 and 314 indicating the provisional sums. When the signal C1\_14 which is the other of the pair of signals C0\_14 and C1\_14 and the exclusive OR signal S0\_15 are inputted,

15 one bit in the first circuit stage 11 are inputted, the first exclusive OR circuit outputs the signal 313 which is one of the pair of signals 313 and 314 indicating the provisional sums. When the signal C1\_14 which is the other of the pair of signals C0\_14 and C1\_14 and the exclusive OR signal S0\_15 are inputted,

20 the second exclusive OR circuit outputs the signal 314 which is the other of the pair of signals 313 and 314 indicating the provisional sums.

Next, a structure of a third circuit stage 13 in the 16-bit adder shown in Fig. 3 will be described. Fig. 7 shows an internal structure of the third circuit stage 13. The third circuit stage 13 is a circuit stage in which  $(N-M+1) = 3$ . Accordingly, assuming that  $N = 4$ ,  $M = 2$  is obtained. In the third circuit stage 13, assuming that  $(N-M) = 2$ , it is divided in a virtual form into  $2^M (= 4)$  sub-circuits P3<sub>1</sub> to P3<sub>4</sub> corresponding to every  $2^{(N-M)}$

25 structure of the third circuit stage 13. The third circuit stage 13 is a circuit stage in which  $(N-M+1) = 3$ . Accordingly, assuming that  $N = 4$ ,  $M = 2$  is obtained. In the third circuit stage 13, assuming that  $(N-M) = 2$ , it is divided in a virtual form into  $2^M (= 4)$  sub-circuits P3<sub>1</sub> to P3<sub>4</sub> corresponding to every  $2^{(N-M)}$

30 bits of the input data.

In the case of such division, two multiplexers 120 are provided corresponding to high  $2^{(N-M-1)}$  ( $= 2$ ) bits in the sub-circuit  $P3_1$  which is a first sub-arithmetic circuit, including inputs from  $2^{(N-M)}$ -th ( $=$  fourth) bits from the least significant bits  $A_0$  and  $B_0$  in the high order direction. The pair of signals 301 and 302 which are the outputs of the carry selector 110 provided for corresponding bits in the second circuit stage 12 which is the preceding circuit stage and indicate the provisional carriers are inputted to the multiplexer provided corresponding to the high order bit. In addition, the pair of signals  $C0_2$  and  $C1_2$  which are the outputs of the conditional cell 101 provided for corresponding bits in the first circuit stage 11 which is the preceding circuit stage and indicate the provisional carriers are inputted to the multiplexer provided corresponding to the low order bit. With respect to these multiplexers, the signal 300 which is outputted from the multiplexer 120 provided for bits in the circuit stage 12, which correspond to  $(2^{(N-M-1)}+1)$ -th ( $=$  third) bits from the high order in the sub-circuit  $P3_1$  is inputted thereto as a selection signal. The multiplexer provided corresponding to the high order bit outputs a signal 401, which is an actual carry signal in accordance with the signal 300. In addition, the multiplexer provided corresponding to the low order bit outputs a signal 400, which is an actual carry signal in accordance with the signal 300.

Also, the  $(2^{(N-1)} - 2^{(N-M-1)})$  ( $= 6$ ) carry selectors 110 are provided corresponding to each high  $2^{(N-M-1)}$  ( $= 2$ ) bits in the sub-circuit  $P3_4$  corresponding to a second sub-arithmetic circuit to which the signals 315 and 316 as the provisional carry signals corresponding to the most significant bits  $A_{15}$  and  $B_{15}$  are inputted and in the corresponding sub-circuits of a third

sub-arithmetic circuit including sub-circuits corresponding to the second sub-circuit  $P3_3$  and the third  $((= 2^M-1)\text{-th})$  sub-circuit  $P3_2$  from the sub-circuit  $P3_4$  in the low order direction. The pair of signals from any one of the conditional cell 101, the carry selector 110, and the converter 140, which are provided for the corresponding bits in the preceding circuit stages are inputted to each of the carry selectors. In addition, the pair of selection signals which are the outputs of the carry selector 110 provided for the bits in the second circuit stage 12, which correspond to  $(2^{(N-M-1)}+1)\text{-th}$  ( $=$  third) bits from the high order in the sub-circuit are inputted to each of the carry selectors. Each of the carry selectors in the second sub-arithmetic circuit ( $P3_4$ ) and the third sub-arithmetic circuit ( $P3_2$  to  $P3_3$ ) selects a pair of signals indicating provisional carriers or the provisional sums in the following circuit stage in accordance with the selection signals and outputs the selected signals.

In other words, the pair of signals 315 and 316 which are the outputs of the carry selector in the second circuit stage 12 are inputted to the carry selector provided corresponding to the high order bit, of the two carry selectors 110 included in the sub-circuit  $P3_4$ . Then, the carry selector performs selection in accordance with the pair of signals 311 and 312 which are the outputs of the carry selector in the second circuit stage 12, which is provided for the bits corresponding to  $(2^{(N-M-1)}+1)\text{-th}$  ( $=$  third) bits from the high order in the sub-circuit  $P3_4$  and outputs a pair of signals 416 and 417. The pair of signals 313 and 314 which are the outputs of the carry selector in the second circuit stage 12 are inputted to the carry selector provided corresponding to the low order bit in the sub-circuit  $P3_4$ . Then, the carry selector performs selection

in accordance with the pair of selection signals 311 and 312 and outputs a pair of signals 414 and 415. Similarly, the pair of signals 309 and 310 which are the outputs of the carry selector in the second circuit stage 12 are inputted to the carry selector provided corresponding to the high order bit, of the two carry selectors 110 included in the sub-circuit  $P3_3$ . Then, the carry selector performs selection in accordance with the pair of selection signals 307 and 308 which are the outputs of the carry selector in the second circuit stage 12, which is provided for the bits corresponding to  $(2^{(N-M-1)}+1)$ -th (= third) bits from the high order in the sub-circuit  $P3_3$  and outputs a pair of signals 408 and 409. The pair of signals  $C0\_10$  and  $C1\_10$  which are the outputs of the conditional cell in the first circuit stage 11 are inputted to the carry selector provided corresponding to the low order bit in the sub-circuit  $P3_3$ . Then, the carry selector performs selection in accordance with the pair of selection signals 307 and 308 and outputs a pair of signals 406 and 407. In addition, the pair of signals 305 and 306 which are the outputs of the carry selector in the second circuit stage 12 are inputted to the carry selector provided corresponding to the high order bit, of the two carry selectors 110 included in the sub-circuit  $P3_2$ . Then, the carry selector performs selection in accordance with the pair of selection signals 303 and 304 which are the outputs of the carry selector in the second circuit stage 12, which is provided for the bits corresponding to  $(2^{(N-M-1)}+1)$ -th (= third) bits from the high order in the sub-circuit  $P3_2$  and outputs a pair of signals 404 and 405. The pair of signals  $C0\_6$  and  $C1\_6$  which are the outputs of the conditional cell in the first circuit stage 11 are inputted to the carry selector provided corresponding to the low order bit in the sub-circuit  $P3_2$ . Then,

the carry selector performs selection in accordance with the pair of selection signals 303 and 304 and outputs a pair of signals 402 and 403.

Also, the two converters 140 are provided corresponding  
 5 to lower  $2^{(N-M-1)}$  ( $= 2$ ) bits in the sub-circuit  $P3_4$  which is the second sub-arithmetic circuit. The pair of signals 311 and 312 and the exclusive OR signal  $S0_{14}$  are inputted to the first converter from the top, of the two converters 140. The pair of signals 311 and 312 are the outputs of the carry selector  
 10 110 provided for corresponding bits in the second circuit stage 12 which is the preceding circuit stage and indicate the provisional carriers. The exclusive OR signal  $S0_{14}$  is outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11. Then, the first  
 15 converter from the top converts the inputted signals into a pair of signals 412 and 413 indicating the provisional sums and outputs the converted signals. The pair of signals  $C0_{12}$  and  $C1_{12}$  and the exclusive OR signal  $S0_{13}$  are inputted to second converter from the top, of the two converters 140. The pair of signals  
 20  $C0_{12}$  and  $C1_{12}$  are the outputs of the carry selector 110 provided for corresponding bits in the first circuit stage 11 which is the preceding circuit stage and indicate the provisional carriers. The exclusive OR signal  $S0_{13}$  is outputted from the conditional cell corresponding to the bit higher by one bit in the first  
 25 circuit stage 11. Then, the second converter from the top converts the inputted signals into a pair of signals 410 and 411 indicating the provisional sums and outputs the converted signals.

Next, a structure of a fourth circuit stage 14 in the 16-bit  
 30 adder shown in Fig. 3 will be described. Fig. 8 shows an internal

structure of the fourth circuit stage 14. The fourth circuit stage 14 is a circuit stage in which  $(N-M+1) = 4$ . Accordingly, assuming that  $N = 4$ ,  $M = 1$  is obtained. In the fourth circuit stage 14, assuming that  $(N-M) = 3$ , it is divided in a virtual  
 5 form into  $2^M (= 2)$  sub-circuits  $P4_1$  and  $P4_2$  corresponding to every  $2^{(N-M)} (= 8)$  bits of the input data.

In the case of such division, four multiplexers 120 are provided corresponding to high  $2^{(N-M-1)} (= 4)$  bits in the sub-circuit  $P4_1$  which is a first sub-arithmetic circuit,  
 10 including inputs from  $2^{(N-M)}$ -th (= eighth) bits from the least significant bits  $A_0$  and  $B_0$  in the high order direction. The pair of signals 404 and 405 which are the outputs of the carry selector 110 provided for corresponding bits in the third circuit stage 13 which is the preceding circuit stage, and which indicate  
 15 the provisional carriers are inputted to the first multiplexer from the top. The signal 401, which is outputted from the multiplexer 120 provided for the bits in the third circuit stage 13, which correspond to  $(2^{(N-M-1)}+1)$ -th (= fifth) bits from the high order in the sub-circuit  $P4_1$ , is used as a selection signal.  
 20 Then, the first multiplexer from the top selects an actual carry signal in accordance with the selection signal and outputs a signal 503. The pair of signals 402 and 403 which are the outputs of the carry selector 110 provided for corresponding bits in the third circuit stage 13 which is the preceding circuit stage, and which indicate the provisional carriers are inputted to the  
 25 second multiplexer from the top. The signal 401 is used as the selection signal. Then, the second multiplexer from the top selects an actual carry signal in accordance with the selection signal and outputs a signal 502. The pair of signals 303 and  
 30 304 which are the outputs of the carry selector 110 provided

for corresponding bits in the second circuit stage 12 which is the preceding circuit stage, and which indicate the provisional carriers are inputted to the third multiplexer from the top. The signal 401 is used as the selection signal. Then, the third  
 5 multiplexer from the top selects an actual carry signal in accordance with the selection signal and outputs a signal 501. The pair of signals C0\_4 and C1\_4 which are the outputs of the conditional cell 101 provided for corresponding bits in the first circuit stage 11 which is the preceding circuit stage, and which  
 10 indicate the provisional carriers are inputted to the fourth multiplexer from the top. The signal 401 is used as the selection signal. Then, the fourth multiplexer from the top selects an actual carry signal in accordance with the selection signal and outputs a signal 500.

15 Also, the  $(2^{(N-1)} - 2^{(N-M-1)})$  ( $= 4$ ) carry selectors 110 are provided corresponding to high  $2^{(N-M-1)}$  ( $= 4$ ) bits in the sub-circuit P4<sub>2</sub> corresponding to a second sub-arithmetic circuit to which the signals 416 and 417 as the carry signals corresponding to the most significant bits A<sub>15</sub> and B<sub>15</sub> are inputted. The  
 20 pair of signals outputted from any one of the conditional cell 101, the carry selector 110, and the converter 140, which are provided for the corresponding bits in the preceding circuit stages are inputted to each of the carry selectors. In addition, the pair of selection signals which are outputted from the carry  
 25 selector 110 provided for the bits in the third circuit stage 13, which correspond to  $(2^{(N-M-1)}+1)$ -th ( $=$  fifth) bits from the high order in the sub-circuit P4<sub>2</sub> are inputted to each of the carry selectors. Each of the carry selectors selects a pair of signal indicating provisional carriers or the provisional  
 30 sums in the following circuit stage in accordance with the

selection signals and outputs the selected signals.

In other words, the pair of signals 416 and 417 which are the outputs of the carry selector in the third circuit stage 13 are inputted to the first carry selector from the top, of  
 5 the four carry selectors 110 included in the sub-circuit  $P4_2$ . Then, the first carry selector from the top performs selection in accordance with the pair of selection signals 408 and 409 which are the outputs of the carry selector in the third circuit stage 13, which is provided for the bits corresponding to  
 10  $(2^{(N-M-1)}+1)$ -th (= fifth) bits from the high order in the sub-circuit  $P4_2$  and outputs a pair of signals 518 and 519. Similarly, the pair of signals 414 and 415 which are the outputs of the carry selector in the third circuit stage 13 are inputted to the second carry selector from the top. Then, the second  
 15 carry selector from the top performs selection in accordance with the pair of selection signals 408 and 409 and outputs a pair of signals 516 and 517. In addition, the pair of signals 412 and 413 which are the outputs of the carry selector in the third circuit stage 13 are inputted to the third carry selector  
 20 from the top. Then, the third carry selector from the top performs selection in accordance with the pair of selection signals 408 and 409 and outputs a pair of signals 514 and 515. In addition, the pair of signals 410 and 411 which are the outputs of the carry selector in the third circuit stage 13 are inputted  
 25 to the lowest order carrier selector, that is, the fourth carry selector from the top. Then, the fourth carry selector from the top performs selection in accordance with the pair of selection signals 408 and 409 and outputs a pair of signals 512 and 513.

30 Also, the four converters 140 are provided corresponding

to low  $2^{(N-M-1)}$  ( $= 4$ ) bits in the sub-circuit  $P4_2$  which is the second sub-arithmetic circuit. The pair of signals 408 and 409 and the exclusive OR signal  $S0\_12$  are inputted to the first converter from the top, of the four converters 140. The pair of signals 408 and 409 are the outputs of the carry selector 110 provided for corresponding bits in the third circuit stage 13 which is the preceding circuit stage and indicate the provisional carriers. The exclusive OR signal  $S0\_12$  is outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11. Then, the first converter from the top converts the inputted signals into a pair of signals 510 and 511 indicating the provisional sums and outputs the converted signals. Similarly, the pair of signals 406 and 407 and the exclusive OR signal  $S0\_11$  are inputted to the second converter from the top. The pair of signals 406 and 407 are the outputs of the carry selector 110 provided for corresponding bits in the third circuit stage 13 which is the preceding circuit stage and indicate the provisional carriers. The exclusive OR signal  $S0\_11$  is outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11. Then, the second converter from the top converts the inputted signals into a pair of signals 508 and 509 indicating the provisional sums and outputs the converted signals. In addition, the pair of signals 307 and 308 and the exclusive OR signal  $S0\_10$  are inputted to the third converter from the top. The pair of signals 307 and 308 are the outputs of the carry selector 110 provided for corresponding bits in the second circuit stage 12 which is the preceding circuit stage and indicate the provisional carriers. The exclusive OR signal  $S0\_10$  is outputted from the conditional cell corresponding to the bit higher by one bit in the first

circuit stage 11. Then, the third converter from the top converts the inputted signals into a pair of signals 506 and 507 indicating the provisional sums and outputs the converted signals. In addition, the pair of signals C0\_8 and C1\_8 and the exclusive OR signal S0\_9 are inputted to the lowest order converter, that is, the fourth converter from the top. The pair of signals C0\_8 and C1\_8 are the outputs of the conditional cell 101 provided for corresponding bits in the first circuit stage 11 which is the preceding circuit stage and indicate the provisional carriers.

The exclusive OR signal S0\_9 is outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11. Then, the fourth converter from the top converts the inputted signals into a pair of signals 504 and 505 indicating the provisional sums and outputs the converted signals.

Fig. 9 is a circuit diagram showing a (N+1)-th (= fifth) circuit stage 15 in the 16-bit adder to which the present invention is applied. The fifth circuit stage 15 includes  $2^{(N-1)}$  (= 8) multiplexers 120 and  $2^{(N-1)}$  (= 8) exclusive OR circuits 130.

The pair of signals 518 and 519 outputted from the first carry selector 110 from the top in the fourth circuit stage 14 are inputted to the multiplexer provided in the bit position corresponding to the most significant bits A\_15 and B\_15 of the input data. Then, the multiplexer selects an output carry signal Cout in accordance with the selection signal 503 outputted from the multiplexer in the fourth circuit stage 14, which corresponds to  $(2^{(N-1)}+1)$ -th (= ninth) bits from the most significant bits of the input data in the low order direction, and outputs the output carry signal Cout to the outside of the adder.

The pair of signals outputted from the carry selector or

the converter which are provided for corresponding bits in the fourth circuit stage 14 are inputted to each of the  $(2^{(N-1)}-1)$  (= 7) multiplexers provided for bits corresponding to 2 to  $(2^{(N-1)}-1)$ -th (= eighth) from the most significant bits of the input data in the low order direction. Then, each of the multiplexers performs selection in accordance with the selection signal 503 outputted from the multiplexer in the fourth circuit stage 14, which corresponds to  $(2^{(N-1)}+1)$ -th (= ninth) bits from the most significant bits of the input data in the low order direction, and outputs a signal indicating an actual bit sum with respect to the bit higher by one bit. That is, the pair of signals 516 and 517 indicating the provisional sums are inputted from the carry selector provided for corresponding bits in the fourth circuit stage to the second multiplexer from the top. Then, the second multiplexer from the top performs selection in accordance with the selection signal 503 which is an actual carry and outputs a signal S\_15 indicating the actual bit sum with respect to the bit higher by one bit to the outside of the adder. The pair of signals 514 and 515 indicating the provisional sums are inputted from the carry selector provided for corresponding bits in the fourth circuit stage to the third multiplexer from the top. Then, the third multiplexer from the top performs selection in accordance with the selection signal 503 and outputs a signal S\_14 indicating the actual bit sum with respect to the bit higher by one bit to the outside. The pair of signals 512 and 513 indicating the provisional sums are inputted from the carry selector provided for corresponding bits in the fourth circuit stage to the fourth multiplexer from the top. Then, the fourth multiplexer from the top performs selection in accordance with the selection signal 503 and outputs

a signal S\_13 indicating the actual bit sum with respect to the bit higher by one bit to the outside. The pair of signals 510 and 511 indicating the provisional sums are inputted from the converter provided for corresponding bits in the fourth circuit stage to the fifth multiplexer from the top. Then, the fifth multiplexer from the top performs selection in accordance with the selection signal 503 and outputs a signal S\_12 indicating the actual bit sum with respect to the bit higher by one bit to the outside. The pair of signals 508 and 509 indicating the provisional sums are inputted from the converter provided for corresponding bits in the fourth circuit stage to the sixth multiplexer from the top. Then, the sixth multiplexer from the top performs selection in accordance with the selection signal 503 and outputs a signal S\_11 indicating the actual bit sum with respect to the bit higher by one bit to the outside. The pair of signals 506 and 507 indicating the provisional sums are inputted from the converter provided for corresponding bits in the fourth circuit stage to the seventh multiplexer from the top. Then, the seventh multiplexer from the top performs selection in accordance with the selection signal 503 and outputs a signal S\_10 indicating the actual bit sum with respect to the bit higher by one bit to the outside. The pair of signals 504 and 505 indicating the provisional sums are inputted from the converter provided for corresponding bits in the fourth circuit stage to the eighth multiplexer from the top. Then, the eighth multiplexer from the top performs selection in accordance with the selection signal 503 and outputs a signal S\_9 indicating the actual bit sum with respect to the bit higher by one bit to the outside.

The signal outputted from the full adder or the multiplexer

which are provided for corresponding bits in the preceding circuit stages and the exclusive OR signal outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11 are inputted to each of the  $2^{(N-1)}$

5 (= 8) exclusive OR circuits 130 provided for bits corresponding to  $(2^{(N-1)}+1)$ -th to  $2^N$ -th (that is, ninth to sixteenth) bits from the most significant bits of the input data in the low order direction. Then, each of the exclusive OR circuits outputs a signal indicating an actual bit sum with respect to the bit higher

10 by one bit to the outside of the adder. That is, when the signal 503 outputted from the multiplexer provided for corresponding bits in the fourth circuit stage 14 and the exclusive OR signal S0\_8 outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11 are inputted

15 to the exclusive OR circuit corresponding to the ninth bits from the most significant bits, the exclusive OR circuit outputs a signal S\_8 indicating the actual bit sum with respect to the bit higher by one bit to the outside. Similarly, when the signal 502 outputted from the multiplexer provided for corresponding

20 bits in the fourth circuit stage 14 and the exclusive OR signal S0\_7 outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11 are inputted to the exclusive OR circuit corresponding to the tenth bits from the most significant bits, the exclusive OR circuit outputs a

25 signal S\_7 indicating the actual bit sum with respect to the bit higher by one bit to the outside. When the signal 501 outputted from the multiplexer provided for corresponding bits in the fourth circuit stage 14 and the exclusive OR signal S0\_6 outputted from the conditional cell corresponding to the bit

30 higher by one bit in the first circuit stage 11 are inputted

to the exclusive OR circuit corresponding to the eleventh bits from the most significant bits, the exclusive OR circuit outputs a signal S\_6 indicating the actual bit sum with respect to the bit higher by one bit to the outside. When the signal 500  
5 outputted from the multiplexer provided for corresponding bits in the fourth circuit stage 14 and the exclusive OR signal S0\_5 outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11 are inputted to the exclusive OR circuit corresponding to the twelfth bits  
10 from the most significant bits, the exclusive OR circuit outputs a signal S\_5 indicating the actual bit sum with respect to the bit higher by one bit to the outside. When the signal 401 outputted from the multiplexer provided for corresponding bits in the third circuit stage 13 and the exclusive OR signal S0\_4  
15 outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11 are inputted to the exclusive OR circuit corresponding to the thirteenth bits from the most significant bits, the exclusive OR circuit outputs a signal S\_4 indicating the actual bit sum with respect to the  
20 bit higher by one bit to the outside. When the signal 400 outputted from the multiplexer provided for corresponding bits in the third circuit stage 13 and the exclusive OR signal S0\_3 outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11 are inputted  
25 to the exclusive OR circuit corresponding to the fourteenth bits from the most significant bits, the exclusive OR circuit outputs a signal S\_3 indicating the actual bit sum with respect to the bit higher by one bit to the outside. When the signal 300 outputted from the multiplexer provided for corresponding bits  
30 in the second circuit stage 12 and the exclusive OR signal S0\_2

outputted from the conditional cell corresponding to the bit higher by one bit in the first circuit stage 11 are inputted to the exclusive OR circuit corresponding to the fifteenth bits from the most significant bits, the exclusive OR circuit outputs  
 5 a signal S\_2 indicating the actual bit sum with respect to the bit higher by one bit to the outside. When the signal Cout\_0 outputted from the full adder 100 provided for corresponding bits in the first circuit stage 11 and the exclusive OR signal S0\_1 outputted from the conditional cell corresponding to the  
 10 bit higher by one bit in the first circuit stage are inputted to the exclusive OR circuit corresponding to the sixteenth bits from the most significant bits, the exclusive OR circuit outputs a signal S\_1 indicating the actual bit sum with respect to the bit higher by one bit to the outside.

15       Next, the operation of the adder of the present invention will be described with reference to the drawings.

In Fig. 4A that shows the first circuit stage 11 shown in Fig. 3, two input data are inputted to the conditional cells 101 for each of identical bits. As shown in Fig. 4B, in each  
 20 of the conditional cells, an AND signal of two input bits Ai and Bi is outputted therefrom as a carry signal C0\_i with respect to the case where no carry is produced from the low order, an OR signal of the two input bits is outputted therefrom as a carry signal C1\_i with respect to the case where carry is produced  
 25 from the low order, and an exclusive OR signal of the two input bits is outputted therefrom as an exclusive OR signal S0\_i corresponding to a bit sum with respect to the case where it is assumed that no carry is produced from the low order. These outputs correspond to the provisional carry signals C0\_1 to C0\_15  
 30 generated in the case where it is assumed that no carry is produced

from the low order, the provisional carry signals  $C1\_1$  to  $C1\_15$  generated in the case where it is assumed that carry is produced from the low order, and the exclusive OR signals  $S0\_1$  to  $S0\_15$ , respectively. Because  $A\_0$ ,  $B\_0$ , and the input carry signal  $Cin$  are inputted from the outside of the adder to the full adder 100 corresponding to the least significant bits, the full adder 100 outputs the actual bit sum signal  $S\_0$  and the actual carry signal  $Cout\_0$  to the high order bit.

Next, in the second circuit stage 12, the provisional carry signals generated in each of the bits are divided corresponding to the sub-circuits  $P2_1$  to  $P2_8$  for every two bits. Each of the sub-circuits  $P2_1$  to  $P2_8$  generates new provisional carriers selected in accordance with the provisional carriers from the bit lower by one bit and outputs the new provisional carriers. The selection of the provisional carriers is performed by the carry selector 110 shown in Fig. 6B. The provisional carriers from the bit lower by one bit, which are inputted as the selection signals to each of the carry selectors in the second circuit stage 12 are generated while assuming the case where carry is produced from the bit further lower by one bit and the case where no carry is produced therefrom. Accordingly, the provisional carry signal outputted from a  $Cout1$  terminal of each of the carry selectors in the second circuit stage 12 is generated while assuming the case where carry is produced from the bit lower by two bits. In addition, the provisional carry signal outputted from a  $Cout0$  terminal of each of the carry selectors is generated while assuming the case where no carry is produced from the bit lower by two bits. That is, because the carry signal  $Cout\_0$  of the least significant bit is the actual carry signal, the multiplexer corresponding to the second bit from the least

significant bit (that is, the multiplexer 120 in the sub-circuit  $P2_1$ ) selects the actual carry signal 300 from the pair of signals  $C0\_1$  and  $C1\_1$  indicating the provisional carriers and outputs the actual carry signal 300.

5        Also, when the pair of signals  $C1\_14$  and  $C0\_14$  and the signal  $S0\_15$  are inputted to the converter 140 in the sub-circuit  $P2_8$ , the converter 14 generates the pair of signals 314 and 313 and outputs them. The pair of signals 314 and 313 correspond to the provisional sums generated while assuming the case where  
10        carry is produced from the low order and the case where no carry is produced therefrom.

Next, in Fig. 7 that shows the third circuit stage 13 shown in Fig. 3, the provisional carriers and the provisional sums which are inputted thereto are divided corresponding to the  
15        sub-circuits  $P3_1$  to  $P3_4$  for every four bits. In the  $k$  ( $k$  is 2, 3, or 4)-th sub-circuit  $P3_k$ , the provisional carriers composed of the pair of signals generated in the high two bits are selected in accordance with the provisional carriers from the third bit from the most significant bit in the sub-circuit  $P3_k$ , so that  
20        new provisional carriers are generated and outputted. Here, the provisional carriers used as the selection signals are generated while assuming the presence or absence of carry from the most significant bit in the sub-circuit  $P3_{k-1}$  lower by one order. Therefore, the provisional carriers and the provisional  
25        sums which are newly generated in the sub-circuit  $P3_k$  and outputted therefrom are all generated while assuming the presence or absence of carry from the most significant bit in the sub-circuit  $P3_{k-1}$  lower by one order. In the lowest order sub-circuit  $P3_1$ , the signal 300 corresponding to the third bit  
30        from the most significant bit is the actual carry signal.

Therefore, the signals 401 and 400 which are selected using the signal 300 as the selection signal by the two multiplexers included in the sub-circuit  $P3_1$  and outputted therefrom are the actual carry signals.

5        Also, when the pair of signals 312 and 311 and the signal  $S0_{14}$  are inputted to the high order converter of the two converters 140 included in the sub-circuit  $P3_4$ , the high order converter generates the pair of signals 413 and 412 and outputs them. When the pair of signals  $C1_{12}$  and  $C0_{12}$  and the signal  
10  $S0_{13}$  are inputted to the low order converter, the low order converter generates the pair of signals 411 and 410 and outputs them. In these converters, the pair of signals 413 and 412 and the pair of signals 411 and 410 correspond to the provisional sums generated while assuming the case where carry is produced  
15 from the low order and the case where no carry is produced therefrom. The output signals 415 to 410 of the sub-circuit  $P3_4$  correspond to the provisional sums corresponding to the high three bits and are generated while assuming the presence or absence of carry from the most significant bit in the sub-circuit  $P3_3$  lower by  
20 one order.

Next, in Fig. 8 that shows the fourth circuit stage 14, the provisional carriers and the provisional sums which are inputted thereto are divided corresponding to the sub-circuits  $P4_1$  and  $P4_2$  for every eight bits. In the sub-circuit  $P4_2$ , the  
25 provisional carriers and the provisional sums which are composed of the pair of signals generated in the high four bits are selected in accordance with the provisional carriers 408 and 409 from the fifth bit from the most significant bit in the sub-circuit  $P4_2$ , so that new provisional carriers and new provisional sums  
30 are generated and outputted. Here, the pair of provisional carry

signals 408 and 409 used as the selection signals are generated while assuming the presence or absence of carry from the most significant bit in the sub-circuit  $P4_1$  lower by one order. Therefore, the provisional carriers and the provisional sums  
 5 which are newly generated in the sub-circuit  $P4_2$  and outputted therefrom are all generated while assuming the presence or absence of carry from the most significant bit in the sub-circuit  $P4_1$  lower by one order. In the low order sub-circuit  $P4_1$ , the signal 401 corresponding to the fifth bit from the most  
 10 significant bit is the actual carry signal. Therefore, all the signals 503, 502, 501, and 500 which are selected using the signal 401 as the selection signal by the four multiplexers included in the sub-circuit  $P4_1$  and outputted therefrom are the actual carry signals.

15 Also, when the pair of signals 409 and 408 and the signal  $S0_{12}$  are inputted to the highest order converter of the four converters 140 included in the sub-circuit  $P4_2$ , the highest order converter generates the pair of signals 511 and 510 and outputs the signals 511 and 510. When the pair of signals 407 and 406  
 20 and the signal  $S0_{11}$  are inputted to the second converter from the top, the second converter generates the pair of signals 509 and 508 and outputs the signals 509 and 508. When the pair of signals 308 and 307 and the signal  $S0_{10}$  are inputted to the third converter from the top, the third converter generates the  
 25 pair of signals 507 and 506 and outputs the signals 507 and 506. When the pair of signals  $C1_8$  and  $C0_8$  and the signal  $S0_9$  are inputted to the fourth converter from the top, the fourth converter generates the pair of signals 505 and 504 and outputs the signals 505 and 504. Here, the pair of signals 511 and 510,  
 30 the pair of signals 509 and 508, the pair of signals 507 and

506, and the pair of signals 505 and 504 correspond to the provisional sums generated to intend the case where carry is produced from the low order and the case where no carry is produced therefrom. That is, the output signals 517 to 504 of the sub-circuit  $P4_2$  correspond to the provisional sums corresponding to the high seven bits and are generated to intend the presence or absence of carry from the most significant bit in the low order sub-circuit  $P4_1$ .

Next, in Fig. 9 that shows the fifth circuit stage 15 which is the final stage as shown in Fig. 3, the provisional sums are inputted to seven multiplexers (second to eighth multiplexers from the top) of the multiplexers provided corresponding to eight bits from the most significant bit. The seven multiplexers perform selection in accordance with the actual carry signal 503 from the ninth bit from the most significant bit and output the signals  $S_{15}$  to  $S_9$  which are the actual bit sum signals to the outside of the adder. The multiplexer corresponding to the most significant bit selects one of the pair of signals 519 and 518 indicating the provisional carriers in accordance with the signal 503 and outputs the output carry signal  $Cout$  as a carry signal generated by adding the two input data to the outside of the adder. With respect to the ninth to sixteenth bits from the most significant bit, the actual carry signals are determined after the operation of the fourth circuit stage 14. Accordingly, as shown in Fig. 9, the eight exclusive OR circuits generate the actual bit sums  $S_8$  to  $S_1$  by exclusive OR operation between the actual carry signals and the bit sum signal  $S0_8$  to  $S0_1$  generated in the first circuit stage 11, and output the generated actual bit sums  $S_8$  to  $S_1$  to the outside of the adder. The signal  $S_0$  generated in the first circuit stage 11 is outputted

as the actual bit sum of the least significant bit to the outside of the adder without processing.

According to the adder of the first conventional example as shown in Fig. 1, the carriers and the sums are generated in the first circuit stage and transferred. In addition, according to the adder of the second conventional example as shown in Fig. 2, the carriers are transferred to generate the actual carry signals and all actual bit sums are generated in the final circuit stage at once. In contrast to those, according to the adder of the present invention, the provisional carriers are converted into the provisional sums in a circuit stage in which the carriers are transferred. Accordingly, according to the adder of the present invention, the number of multiplexers and the number of input and output wirings for the multiplexers can be reduced as compared with the adder of the first conventional example in which the carriers and the sums are generated for all bits and transferred. Thus, power dissipation can be reduced. In addition, the adder of the present invention can be realized by the number of circuit stages equal to that in the first conventional example (that is, the number of circuit stages smaller than that in the second conventional example by one). Thus, as compared with the adder of the second conventional example, it is possible that adding is executed at high speed.

The number of multiplexers necessary to construct the adder of the first conventional example is compared with the number of multiplexers necessary to construct the adder of the present invention. In the case of the 16-bit adder, although 75 multiplexers are required for the first conventional example, the adder of the present invention can be constructed by circuits corresponding to 71 multiplexers. In the case of the 32-bit

adder, although 186 multiplexers are required for the first conventional example, the adder of the present invention can be constructed by circuits corresponding to 175 multiplexers. The case of the 32-bit adder will be itemized in detail. In  
5 the present invention, the number of multiplexers is reduced from 186 in the first conventional example to 129. However, because 46 converters in total are added to generate bit sums in a circuit stage. As a result, 11 multiplexers can be omitted. Further, even in the case of each of the conditional cells,  
10 although two bit sum signals are required as the provisional sums in the first conventional example, only one exclusive OR signal may be generated in the present invention. Thus, according to the present invention, the number of transistors necessary to construct the conditional cells can be reduced and  
15 power dissipation can be reduced in view of this point. Note that, with respect to count of the number of circuits corresponding to the multiplexers, it is assumed that those circuits are composed of pass transistors, the carry selector and the converter each are converted to 2 multiplexers, and the  
20 exclusive OR circuit is converted to 1 multiplexer.

Also, the number of circuit stages necessary to construct the adder of the second conventional example is compared with the number of circuit stages necessary to construct the adder of the present invention. In the case where the 16-bit adder  
25 is constructed, although 6 circuit stages are required for the adder of the second conventional example, the adder of the present invention can be constructed by 5 circuit stages. In the case of the 32-bit adder, although 7 circuit stages are required for the adder of the second conventional example, the adder of the  
30 present invention can be constructed by 6 circuit stages. Thus,

the number of logic stages in a critical path of the adder of the present invention can be reduced by one as compared with that of the adder of the second conventional example, and the adder of the present invention can be realized by the number  
5 of logic stages equal to that in the adder of the first conventional example. Here, the number of logic stages indicates the sum total of the numbers of conditional cells, multiplexers, carry selectors, converters, and exclusive OR circuits, which are located on a path on which the carriers or the sums are transferred  
10 from the first circuit stage to the final circuit stage.

Note that, although the embodiment of the present invention is described with reference to the 16-bit adder, the present invention is not limited to the 16-bit adder. According to the present invention, with respect to a  $2^N$ -bit adder, although  
15 effects with respect to reduction in power and an increase in speed are unremarkable in the case of  $N \leq 2$ , the effects with respect to reduction in power and an increase in speed are produced in the case of  $N \geq 3$ .

As described above, the adder of the present invention  
20 has the same number of circuit stages as in the first conventional example. Thus, there is a remarkable effect that the adder can operate in low power by reducing the number of unit cells such as multiplexers and the number of wirings as compared with the first conventional example while operation at the same speed  
25 as in the first conventional example (that is, at higher speed than in the second conventional example) is maintained.